

“DISCUSSION” COMMON IN SECONDARY MATH CLASSES

Initiation – Response – Feedback

Teacher [Initiation]: What kind of mathematical relationship does this equation $[y = 2x + 5]$ show?

Student [Response]: A linear relationship.

Teacher [Feedback]: Okay. It's a linear relationship.

Funneling

Teacher: (0, 0) and (4, 1) [are two points on the line in graph B.] Great. What's the slope?

[Long pause – no response from students.]

Teacher: What's the rise? You're going from 0 on the y [axis] up to 1? What's the rise?

Students: 1.

Teacher: 1. What's the run? You're going from 0 to 4 on the x [axis]?

Students: 4.

Teacher: So the slope is ____?

Students: 0.25 [in unison with the teacher.]

Teacher: And the y -intercept is?

Students: 0.

Teacher: So, $y = \frac{1}{4}x$? Or $y = 0.25x$ would be your equation.

What's going on that is leaving this discussion shallow? Can you think of anything the teacher could do to deepen the discussion?

3 Norms I Try to Establish in My Courses

Norm or Value	What does this mean?	What do I try to do as an instructor?
We are a community of learners.	<ul style="list-style-type: none"> We know each other's names. We use each other's names when talking about ideas. We address each other, not just the professor. We make sense of and address each other's thinking, in addition to offering up our own ideas. We see each other as intellectual resources. When we turn to each other to answer our questions, we all develop a deeper understanding. 	<ul style="list-style-type: none"> I spend a little time in the first 3 classes with name activities. I have them take a name quiz. I call on students by name. I refer to idea's brought up in class by the student's name. "What about Megan's idea?" I remind them to use each other's names, and that it's ok to ask someone their name if you forget. I remind them about body language. I stand to the side or in back of the class when a student is presenting. When a student has a question, I ask the entire class what they think. When students work in small groups, I ask individuals, "Cameron, did you follow what Lizzie said? Can you explain it in your own words? Could you ask her to explain it again?"
Mistakes, mis-understandings, confusion, and half-formed ideas are all valuable to talk about.	<ul style="list-style-type: none"> Teachers often say, if you have that question then someone else probably does, too – but even if someone doesn't have that question, that question might never have occurred to them. Unpacking confusion helps us all to understand an idea in a more complete and complex way. The way the discipline of mathematics grew is through examining areas of uncertainty and confusion, of pushing each other to be more precise, of offering ideas that are only half-formed. (Proofs and Refutations by Lakatos, for example.) 	<ul style="list-style-type: none"> I pursue incorrect ideas by asking what others think. We spend time in class figuring out whether something is right or wrong. After a discussion, I bring attention to what we learned by an incomplete or incorrect idea brought up by a student. I thank the student. Students have time to work in small groups. As I visit, if I hear an interesting beginning of an idea, question, or incorrect idea, I ask the student to bring it up to the whole class. I reiterate that the first time you say something, it can come out confusing, but we work together to say it over and over again until it becomes clearer. I ask students to repeat their peers' ideas in their own words.
Everyone is expected to contribute	<ul style="list-style-type: none"> Everyone contributes, everyday. A contribution can be "I don't understand what George is saying." That's valuable because it pushes George to be more precise – and gives us all a chance to try to understand George's idea again. 	<ul style="list-style-type: none"> I use wait time. Sometimes I say, "I want to hear from someone who hasn't spoken yet today." I warm-call students. That means, when they are in small groups, I tell them that I want them to be the reporter on a particular idea. I tell them to try to explain it to their small group as a dry run. I cold call. Sometimes I cold call on a group, using the name of a student who hasn't spoken that day. Sometimes I directly cold call. When I cold call, it's an open question – "What do you think of Cassie's idea?" It's ok if they don't understand Cassie's idea – then I prompt them to ask Cassie to explain the idea again.

